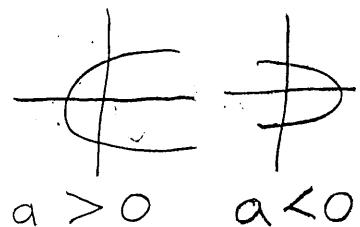


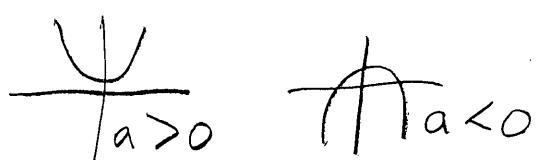
# Conics

- Parabola

$$(y - k)^2 = 4a(x - h)$$



$$(x - h)^2 = 4a(y - k)$$

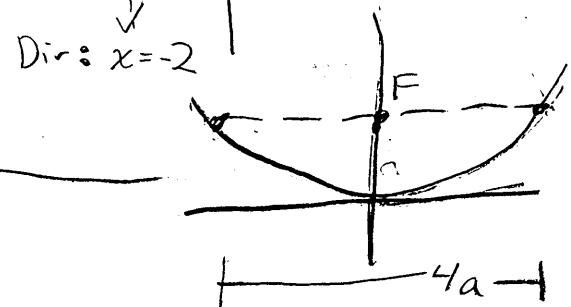
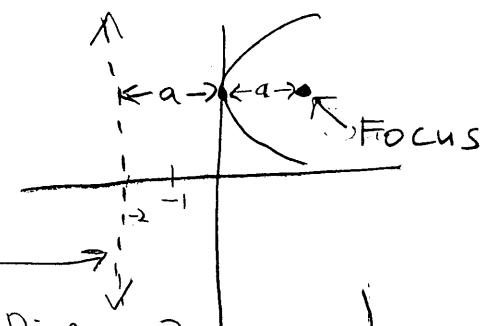


Vertex -  $V(h, k)$

Focal distance =  $a$

Directrix is "a" units  
from the vertex.

$4a$  - distance through  
the focus



- Circle

$$(x - h)^2 + (y - k)^2 = r^2$$

Center -  $(h, k)$

Radius -  $r$

## Conics (Cont'd)

### - Ellipse

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

Graph "a" units  
in the x direction

Graph "b" units  
in the y direction

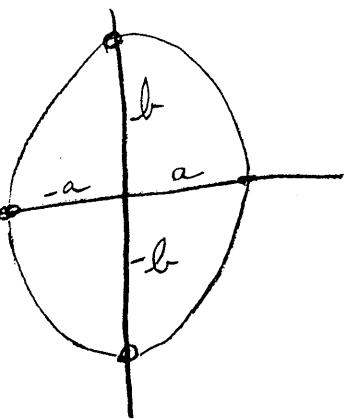
$$c^2 = a^2 - b^2$$

$$\text{or } c^2 = b^2 - a^2$$

↑

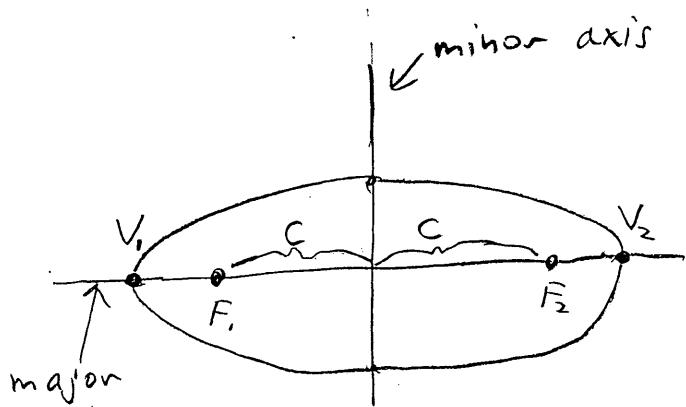
Larger number goes first.

c is the focal length.



$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$$

Center -  $(h, k)$



Foci are always in the long direction, meaning  
on the major axis.

Vertices are on the major axis. (See  $V_1$  &  $V_2$ )

Length of the major axis is the distance from  
 $V_1$  to  $V_2$ .

Sum of focal radii is the distance from  $V_1$  to  $V_2$ .

## Conics (Cont.)

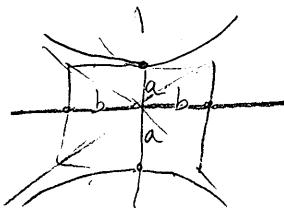
### - Hyperbola

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1 \quad \rightarrow a \quad | \quad a$$

$$c^2 = a^2 + b^2$$

$c$  is the focal length

$$\frac{y^2}{a^2} - \frac{x^2}{b^2} = 1$$

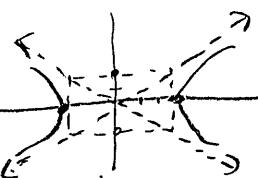


If  $x^2$  term is first, graph cuts through the  $x$ -axis.

If  $y^2$  term is first, graph cuts through the  $y$ -axis.

Asymptotes

$$y = \pm \frac{b}{a}x$$



where "b" is change in  $y$   
and "a" is change in  $x$

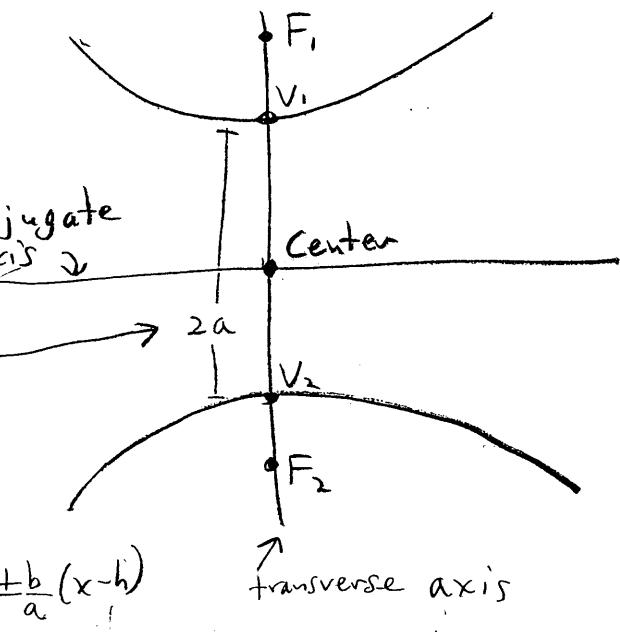
Difference of focal radii is  $2a$ .

$$\frac{(x-h)^2}{a^2} - \frac{(y-k)^2}{b^2} = 1$$

Center  $(h, k)$ , Asymptotes:  $y - k = \pm \frac{b}{a}(x - h)$

conjugate axis

$2a$



$$\frac{(y-k)^2}{a^2} - \frac{(x-h)^2}{b^2} = 1$$

Center  $(h, k)$ , Asymptotes:  $y - k = \pm \frac{a}{b}(x - h)$

change in  $y$

$\frac{a}{b}$

change in  $x$