<u>unit multiplier</u> (**yoo**-nit **mul**-tuh-plye-ur) - a fraction that is equal to one, and contains units in the numerator and denominator. You multiply it, in conversion problems.

Examples:

| 7 days | 1 week | 365 days | 1 year |
|--------|--------|----------|----------|
| 1 week | 7 days | 1 year | 365 days |

To make a unit multiplier you take a relationship between units, and make it a fraction. For example the relationship between days and weeks is there are 7 days in one week. You can make two different unit multipliers using this relationship.

7 days or 1 week 7 days

Say each word out loud and write it in the blank.

| unit | | |
|------------|--|--|
| multiplier | | |

Write the definition in your own words.

unit multiplier

Write two sentences using "unit multiplier."

unit multiplier

1.

2.

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Write two different unit multipliers for each of the following.

| There are 52 weeks in one year. | S |
|--|--------------|
| There are 60 minutes in one hour. | |
| In one minute there is 60 seconds. | |
| In one year there are 365 days. | |
| | |
| Write down 4 examples of unit multipliers using US or Mo | etric units. |
| 1. | |
| 2. | |
| 3. | |
| 4. | |
| | |
| | |

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When studying fractions you learned that fractions with the same numerator and denominator equal one.

Examples:

$$\frac{4}{4} = 1$$
 $\frac{17}{17} = 1$

$$\frac{17}{17} = 1$$

Solve

1.
$$\frac{3}{3}$$

1.
$$\frac{3}{3} =$$
 2. $\frac{54}{54} =$ 3. $\frac{153}{153} =$

Study the following.

When you have the same units in a numerator and denominator, that also equals one.

Example: weeks = 1

$$\underline{\text{weeks}} = 1$$

weeks

Solve

1.
$$\frac{\text{days}}{\text{days}} =$$

$$\frac{\text{days}}{\text{days}} = 2. \quad \frac{\text{years}}{\text{years}} =$$

3.
$$\underline{\text{minutes}} = \\ \text{minutes}$$

Study the following.

Anything times 1 is itself.

Examples: $5 \times 1 = 5$ $99 \times 1 = 99$

Solve

1.
$$4 \times 1 =$$

2.
$$6 \times 1 =$$

3.
$$14 \times 1 =$$

Anything divided by one is itself.

Examples:
$$\underline{2} = 2$$
 $\underline{5} = 5$ $\underline{\text{days}} = \text{days}$

$$\frac{5}{1} = 5$$

$$\frac{\text{days}}{1} = \text{days}$$

Solve

1.
$$\frac{5}{1} =$$
 2. $\frac{17}{1} =$ 3. $\frac{\text{years}}{1} =$

4.
$$\underline{\text{minutes}} = 1$$

$$5. \quad \frac{\text{seconds}}{1} =$$

Study the following.

You can also write in a denominator of 1 to help you with other calculations.

Examples:
$$2 = \frac{2}{1}$$
 $47 = \frac{47}{1}$ seconds = $\frac{\text{seconds}}{1}$

$$47 = \underline{47}$$

$$seconds = \frac{seconds}{1}$$

Write with a denominator of 1.

4.
$$days = 5$$
.

When you are multiplying fractions, and you have the same number in one of the numerators as in one of the denominators, you can cross both numbers out and make them 1's.

This is sometimes called canceling.

Then multiply the remaining numbers across.

Example:

$$\frac{3\times5\times8}{8}$$

$$\underbrace{\frac{3}{8}}_{2} \times \underbrace{\frac{5}{8}}_{7}$$

$$\frac{3\times5}{1}\times\frac{1}{2}$$

answer:

Solve.

$$1. \qquad \frac{4 \times 2 \times 7}{9 \times 3} = \frac{1}{4}$$

$$2. \qquad \frac{5}{2} \times \frac{1}{5} \times \frac{7}{3} =$$

Canceling also applies to units.

Example:
$$\frac{14 \text{ days}}{1} \times \frac{1 \text{ week}}{7 \text{ days}}$$

$$\frac{14 \times 1}{1} \times \frac{1 \text{ week}}{7 \times 1}$$

$$\frac{14}{1} \times \frac{1 \text{ week}}{7} = \frac{14 \text{ weeks}}{7} = 2 \text{ weeks}$$

Usually when you cancel units you just cross them out. You do not need to replace them with a 1.

Example:

$$\frac{4 \text{ minutes} \times 60 \text{ seconds}}{1 \text{ minute}} = \frac{4 \text{ minutes}}{1 \text{ minute}} \times \frac{60 \text{ seconds}}{1 \text{ minute}} = \frac{4 \times 60 \text{ seconds}}{1 \text{ minute}} = \frac{240 \text{ seconds}}{1 \text{ minute}} =$$

Solve.

1.
$$\frac{48 \text{ hours}}{1} \times \frac{1 \text{ day}}{24 \text{ hours}} =$$

2.
$$\frac{3 \text{ hours}}{1} \times \frac{60 \text{ minutes}}{1 \text{ hour}} =$$

3.
$$\frac{120 \text{ minutes}}{1} \times \frac{1 \text{ hour}}{60 \text{ minutes}} =$$

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There are 4 steps to convert units of measure.

- Step 1: Write down the original number with the units an numerator and a 1 as denominator.
- Step 2: Figure out the two possible unit multipliers.
- Step 3: Select the unit multiplier that will result in the original units being canceled. Write it multiplied by step 1.

Step 4: Solve.

Example: Problem: Convert 21 days to weeks.

Step 3:
$$\frac{21 \text{ days}}{1} \times \frac{1 \text{ week}}{7 \text{ days}}$$

Step 4:
$$\frac{21 \text{ days}}{1} \times \frac{1 \text{ week}}{7 \text{ days}} = \frac{21 \text{ weeks}}{7} = 3 \text{ weeks}$$

Convert 4 minutes to seconds, and show all 4 steps.

Step 1:

Step 2:

Step 3:

Step 4:

| Convert 104 weeks to years, and show all 4 steps. |
|---|
| Step 1: |
| Step 2: |
| Step 3: |
| Step 4: |
| Convert 6 hours to minutes, and show all 4 steps. |
| Step 1: |
| Step 2: |
| Step 3: |
| Step 4: |
| Convert 180 hours to minutes, and show all 4 steps. |
| Step 1: |
| Step 2: |
| Step 3: |
| Step 4: |

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US Measurement Conversions. Convert the following using steps 1 to 4.

CHAPTER 16 – ADVANCED CONVERSIONS

| 10. | 8000 pounds = | tons |
|----------|---------------|------|
| . | coco pountas | COIL |

Metric Measurement Conversions. Convert the following using steps 1 to 4.

1. 6 centimeters = _____millimeters

2. 500 centimeters = ______meters

3. 2000 grams = _____kilograms

4. 7 liters = _____ milliliters

5. 2 kilometers = _____ meters

6. 40 millimeters = centimeters

7. 4 kiloliters = _____liters

8. 7000 liters = _____kiloliters

9. 2000 meters = _____kilometers

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| 10. | 4 centimeters = | millimeters |
|-----|-----------------|---------------------------------|
| 11. | 5 kilograms = _ | grams |
| 12. | 4000 meters = _ | kilometers |
| 13. | 5000 grams = _ | kilograms |
| 14. | 6000 liters = _ | kiloliters |
| 15. | 2 liters = | milliliters |
| 16. | 2 meters = | centimeters |
| 17. | 12 grams = | milligrams |
| 18. | 400 centimeters | $S = \underline{\qquad}$ meters |